The optical/UV excess of isolated neutron stars in the RCS model

H. Tong¹, R. X. Xu² and L. M. Song¹

- ¹ Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China; haotong@ihep.ac.cn
- ² School of Physics and State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, China

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Abstract The X-ray dim isolated neutron stars (XDINSs) are peculiar pulsar-like objects, characterized by their very well Planck-like spectrum. In studying their spectral energy distributions, the optical/UV excess is a long standing problem. Recently, Kaplan et al. (2011) have measured the optical/UV excess for all seven sources, which is understandable in the resonant cyclotron scattering (RCS) model previously addressed. The RCS model calculations show that the RCS process can account for the observed optical/UV excess for most sources . The flat spectrum of RX J2143.0+0654 may due to contribution from bremsstrahlung emission of the electron system in addition to the RCS process.

Key words: pulsars: individual: (RX J0420.0-5022, RX J0720.4-3125, RX J0806.4-4123, RX J1308.6+2127, RX J1605.3+3249, RX J1856.5-3754, RX J2143.0+0654), stars: neutron

1 INTRODUCTION

The seven X-ray dim isolated neutron stars (XDINSs) are puzzling pulsar-like compact stars. They are characterized by their very well Planck-like spectrum, and then they are good specimen for neutron star cooling, atmospheric and equation of state studies (Tong et al. 2007,2008; review Turolla 2009). Additionally, these sources may also have some relations with other classes of pulsar-like objects, e.g., magnetars and rotating radio transients, etc (Tong et al. 2010).

The spectral energy distributions of XDINSs show that their optical and UV emissions are above the extrapolation of the X-ray blackbodies, i.e., optical/UV excess. This excess of XDINSs is a long standing problem which may be related to the equation of state of neutron stars (Xu 2002, 2009). Previously, only two sources (RX J1856.5-3754 and RX J0720.4-3125) have both optical and UV data (van Kerkwijk & Kaplan 2007). Recently, Kaplan et al. (2011) have presented results of the optical and UV emission for all seven sources. They also find that the source RX J2143.0+0654 has a very flat spectrm ($F_{\nu} \propto \nu^{\alpha}$, $\alpha \sim 0.5$). This new observation requires updated modeling of existing theoretical models.

Tong et al. (2010) have considered the resonant cyclotron scattering (RCS) in pulsar magnetospheres as the origin of optical/UV excess in XDINSs, i.e., the RCS model. This model can explain the observations of RX J1856.5-3754 and RX J0720.4-3125 (Tong et al. 2010). Considering the recent observational progress, we apply the RCS model to all seven XDINSs in this paper.

Section 2 is summary of the RCS model. Its application to XDINSs is treated in Section 3. Discussions and conclusions are presented in section 4.

2 THE RCS MODEL: A SUMMARY

Tong et al. (2010) have considered the RCS model for the origin of optical/UV excess in XDINSs. It has the following three key points.

- 1. In analogy with magnetospheric study of magnetars and rotating radio transients, also similar to the "electron blanket" of neutron stars (Ruderman 2003), there may also be a dense electron system in closed field line regions of XDINSs. We call it the "pulsar inner radiation belt" (since it is not far away from the central star), in comparison with the "pulsar radiation belt" proposed by Luo & Melrose (2007) (It may be called the "pulsar outer radiation belt", since it is near the light cylinder far away from the central star).
- 2. The scatterings between surface X-ray photons and the electron system are modeled three dimensionally using the Kompaneets equation method. Numerical calculations show that there exist both down scattering and up scattering of the RCS process. The existence of down scattering of RCS process is crucial for its application to XDINSs.
- 3. The application of down scattering of RCS process to XDINSs can explain its optical/UV excess problem.

The Kompaneets equation (photon diffusion equation) for RCS process is (Tong et al. 2010):

$$\left(\frac{\partial n}{\partial t}\right)_{\text{RCS}} = \frac{kT_e}{m_e c^2} \frac{1}{x^2} \frac{\partial}{\partial x} \left\{ x^4 \frac{\tau_{\text{RCS}}}{r_1 - r_2} c g_\theta \left[\frac{\partial n}{\partial x} + n(1+n) \right] \right\}.$$
(1)

Here, n is the photon occupation number, its evolution with time (which corresponds to spectra change) is determined by the right hand side of equation (1). x is the dimensionless photon frequency in units of electron temperature, τ_{RCS} is the RCS optical depth. In order to calculate the RCS modified blackbody spectrum, four input parameters are needed: the neutron star surface temperature, the temperature and density of the electron system, and a normalization constant.

For photons in a certain frequency range, e.g., from optical to soft X-ray, only electrons in a specific radius range will contribute to the RCS process. The electron system may extend to much larger radius, however the electrons there will not contribute to the RCS process (Tong et al. 2010). On the other hand, the electrons will radiate thermal bremsstrahlung emission, which indeed depends on the radial extension of the electron system. The inclusion of thermal bremsstrahlung process in addition to the RCS process will result in a flat optical spectrum.

3 APPLICATION OF THE RCS MODEL TO X-RAY DIM ISOLATED NEUTRON STARS

The application of RCS model to RX J1856.5-3754 is shown in figure 1. Model calculations for the rest six sources are shown in figure 2. The input parameters of RCS model are given is table 1. The neutron star surface temperature $T_{\rm x}$ is chosen as the temperature of the X-ray blackbody (from table 2 in Kaplan et al. 2011) and is kept fixed during the fitting process. The normalization is the radius of the radiation region over the source distance. For example, for RX J1856.5-3754, $R/d=10/0.16 ({\rm km/kpc})$. It means that for a source distance $0.16~{\rm kpc}$ the radius of the radiation region is $10~{\rm km}$. All distance data are from table 4 in Kaplan & van Kerkwijk (2009). The electron temperature $T_{\rm e}$ is about $0.5~T_{\rm x}$ or lower. The electron number density $N_{\rm e}$ is around $1.5\times10^{12}~{\rm cm}^{-3}$. The neutral hydrogen column density $N_{\rm H,rcs}$ is one and a half or two times that of blackbody fit to the X-ray data. Considering that for all seven XDINSs, their surface magnetic field, surface temperature, radiation region, X-ray luminosity, and distance are all similar to each other (Kaplan & van Kerkwijk 2009). Meanwhile, they all have an optical/UV excess of order ten etc (Kaplan et al. 2011). Hence, these seven sources are similar to each other observationally. As a consequence of this, the RCS model parameters for these sources are also similar to each other.

The two sources RX J1605.3+3429 and RX J2143.0+0654 have flat optical/UV spectra (especially for RX J2143.0+0654). For most sources, a power law fit to the optical/UV data gives $F_{\nu} \propto \nu^{\alpha}$, with $\alpha \sim 2$ implying a thermal origin. While for RX J2143.0+0654, $\alpha \sim 0.5$ (table 5 in Kaplan et al. 2011). The flat spectrum of RX J2143.0+0654 indicates that nonthermal processes are involved in its

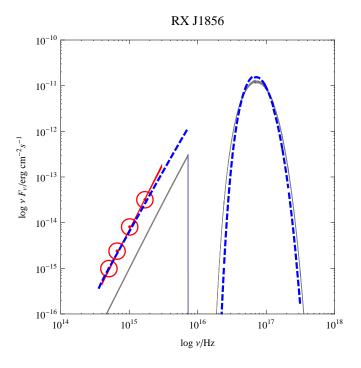


Fig. 1 Spectral energy distributions of RX J1856.5-3754 and RCS model calculations. The gray region is the X-ray blackbody and its extrapolation to the optical and UV range, including $1-\sigma$ uncertainties. The red region is the power law fit to the optical and UV data, including $1-\sigma$ uncertainties. The red circles are observational data points, only central values are included. All the observational data are from Kaplan et al. (2011). The gap between optical/UV and X-ray is due to neutral hydrogen absorption. The dashed line is RCS model calculation (Tong et al. 2010).

optical/UV emission. Noting that the bremsstrahlung emission has a flat spectrum, we propose that the flat spectrum of RX J2143.0+0654 may due to thermal bremsstrahlung emission of the electron system in addition to the RCS process.

From table 1, the temperature and density of the electron system are known. Once its radial extension is given, we can calculate its bremsstrahlung flux at earth (Rybicki & Lightman 1979). The outer radius of the electron system $r_{\rm out}$ determines the relative importance of the bremsstrahlung component. For RX J1605.3+3429 and RX J2143.0+0654, $r_{\rm out}$ is determined in order to obtain a flat optical spectrum. For the rest five sources, no bremsstrahlung component is needed. Therefore, an upper bound on $r_{\rm out}$ is given. The rotation periods of XDINSs are about $10\,{\rm sec}$. Therefore, the radial extension of the electron system is at most five percent of the light cylinder radius, i.e., near the central star. This is why we call it "pulsar inner radiation belt".

When the electron number density varies with radius, e.g, $N_e(r) = N_e \times (r/R_{\rm ns})^{-\alpha}$, the fitting results will be different from the uniform density case as considered above. In order for electrons in a large space range all contributing to the bremsstrahlung process, the power index α should not be significantly larger than 1, i.e., $0 < \alpha < 1$ is required for RX J1605.3+3249 and RX J2143.0+0654. While for the rest five sources, we do not see such a bremsstrahlung component. This is due to either a small radial extension of the electron system or the electron number density there decreases with radius very rapidly, i.e., $\alpha > 1$. The formation of the electron system is discussed in the appendix.

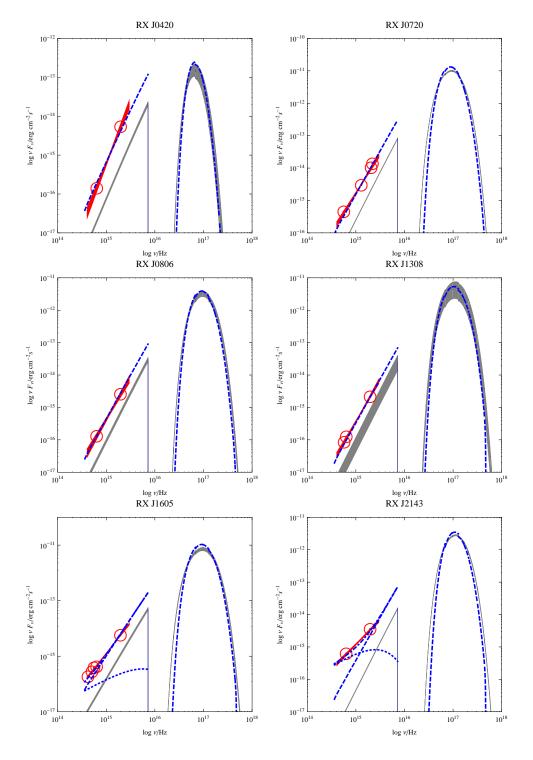


Fig. 2 Calculations for RX J0420.0-5022, RX J0720.4-3125, RX J0806.4-4123, RX J1308.6+2127, RX J1605.3+3249 and RX J2143.0+0654. The same as figure 2. All observational data are from Kaplan et al. (2011). The dashed line is the RCS model calculation (Tong et al. 2010). The dotted line is the contribution from electron thermal bremsstrahlung. The dot-dashed line is the sum of bremsstrahlung and RCS component. The bremsstrahlung component is needed only in the case of RX J1605.3+3249 and RX J2143.0+0654.

Table 1 Input Parameters of the RCS Model. Column one to seven are source name, neutron star surface temperature, normalization, electron temperature, electron density, neutral hydrogen column density, and outer radius of the electron system, respectively. See text for details.

Source	$T_{\rm x}$	R/d	$T_{\rm e}$	$N_{ m e}$	$N_{ m H,rcs}$	$r_{ m out}$
	(eV)	(km/kpc)	(eV)	$(10^{12} \mathrm{cm}^{-3})$	(10^{20}cm^{-2})	$(10^9 {\rm cm})$
J0420	45.0	9/0.345	22.5	2.0	3.0	< 1.2
J0720	88.4	9/0.36	35.4	1.6	2.1	< 2.2
J0806	87.2	3.5/0.25	43.6	1.6	2.6	< 1.2
J1308	102	5.5/0.5	51	1.4	2.7	< 1.8
J1605	92.6	7.5/0.39	23.2	1.8	2.0	1.2
J1856	63.5	10/0.16	25.4	1.8	1.7	< 1.5
J2143	104	4.5/0.43	10.4	1.5	4.6	2.2

4 DISCUSSIONS AND CONCLUSIONS

In the discussion section of Kaplan et al. (2011), they also mentioned the RCS process, which they refer to the paper of Lyutikov & Gavriil (2006). However, as pointed in Tong et al. (2010), the one dimensional treatment of Lyutikov & Gavriil (2006) can only result in up scattering. While the optical/UV excess of XDINSs is of "soft excess" in nature, which requires down scattering process. This is the reason that Tong et al. (2010) modeled the RCS process three dimensionally and employed the Kompaneets equation method.

The RCS model can explain the spectral energy distributions of XDINSs in a wide parameter space. Meanwhile, since the surface X-ray photons are scattered by a shell of electrons, this will result in a low pulsation amplitude naturally. The X-ray spectra are Planck-like with no high energy tails. This may imply that XDINSs are possibly quark stars (Xu 2002,2009). At the same time, the possible features may be proton cyclotron lines or electron cyclotron lines far in the magnetosphere (Turolla 2009).

From figure 3 in Kaplan et al. (2011) we see that for RX J2143.0+0654 we have only two data points at present. Future more optical and UV data will tell us whether its spectrum is really so flat or not. Moreover, with more data points we can know whether there is curvature in the optical/UV spectrum and whether there are more spectra components in addition to the power law component. The electron thermal bresstrahlung component has a flat spectrum in the IR/optical range, with a flux about $0.1\mu Jy$ for RX J2143.0+0654. This flux is much lower than the H-band flux upper limit $(1.6\mu Jy \text{ at } 1.65 \mu m, \text{Lo Curto et al. 2007})$. Therefore in order to verify whether the flat spectrum of RX J2143.0+0654 is due to thermal bremsstrahlung process, deeper optical/UV and IR observations are required.

The electron system cools down via the bremsstrahlung process (possibly also via free-bound transitions, i.e., recombination process). Therefore, the central star has to continually heat the electron system and ionize it. This is similar to the "Strömgren sphere" around early-type stars (Dyson & Williams 1980). The size of the ionized region is $(3S/4\pi N_e^2\beta_2)^{1/3}$ (Dyson & Williamas 1980), where S is the ionizing photon number flux of the central star, N_e is the electron number density (assuming fully ionized hydrogen plasma), β_2 is the recombination coefficient. Similar calculations show that the size of the ionized region is $\sim 10^{10}$ cm, to order of magnitude consistent with the outer radius used in table 1.

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Appendix A: FORMATION OF THE ELECTRON SYSTEM

The electron system may be formed similarly to the "injection through ionization" process (Luo & Melrose 2007). Assuming a neutron star whose mass is $1.4 \, M_{\odot}$, radius $10 \, \mathrm{km}$ and spatial ve-

locity $100\,\mathrm{km\,s^{-1}}$, it will accrete interstellar medium or circumpulsar material at a rate $\dot{M}=2\pi(GM)^2V^{-3}\rho_\mathrm{ISM}\sim2\times10^8\,\mathrm{g\,s^{-1}}$ (Frank et al. 2002), where the density of interstellar medium is assumed to be $10^{-24}\,\mathrm{g\,cm^{-3}}$. Since the accretion rate is rather low, the corresponding Alfvén radius $r_\mathrm{m}\sim4\times10^{11}\,\mathrm{cm}$ is larger than the light cylinder radius and corotation radius. Only a small fraction of the accreted matter can fall onto the neutron star through diffusion process, similar to the propeller case (Ertan et al. 2007). Since we are considering diffusion process along magnetic field lines, the diffusion properties are not affected by the presence of magnetic field. Assuming the plasma deflection length as the typical mean free path (Frank et al. 2002), the particle flux of the diffusion process is $F=D|\nabla n_\mathrm{ISM}|\sim\frac{1}{3}\lambda v_\mathrm{rms}\frac{n_\mathrm{ISM}}{r_\mathrm{m}}\sim10^6\,\mathrm{cm^{-2}\,s^{-1}}$, where D is diffusion coefficient, λ the mean free path $\sim10^{12}\,\mathrm{cm},\,v_\mathrm{rms}$ the typical particle velocity $\sim10\,\mathrm{km\,s^{-1}}$, and n_ISM the interstellar medium number density $\sim1\,\mathrm{cm^{-3}}$. With such a diffusion flux, the corresponding accretion rate is about two hundred times smaller than the total Bondi-Hoyle accretion rate given above. The time scale for the formation of the electron system is about $4\times10^3\,\mathrm{yr}\ll\tau_c$, where τ_c is the pulsar characteristic age $\approx4\times10^6\,\mathrm{yr}$ for RX J2143.0+0654. When the diffused plasma comes to the vicinity of the neutron star, they will diffusion across magnetic field lines and enter into the pulsar closed field regions. The plasma system of the RCS model may be formed. The maximum particle number density that can be confined by the magnetic field at r_out is (i.e., the kinematic energy density and magnetic one are in equilibrium): $B(r_\mathrm{out})^2/(8\pi k T_\mathrm{e})\sim10^{16}\,\mathrm{cm^{-3}}\gg N_\mathrm{e}$. The plasma system can be confined by the magnetic field.

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